## **Rules of Logarithms**

Just like there are rules of exponents, there are rules of logarithms. They should have already been explained to you elsewhere, so here we'll just list them.

 $\begin{array}{ll} (1) & \log_r(AB) = \log_r A + \log_r B. \\ (2) & \log_r \frac{A}{B} = \log_r A - \log_r B. \\ (3) & \log_r(A^B) = B \log_r A. \\ (4) & \log_r r^A = A. \\ (5) & r^{\log_r A} = A. \end{array}$ 

These rules can be used to simplify expressions.

(1) Use the rules of logarithms to write the following expressions as logarithms of one quantity with coefficient 1.

(a) 
$$\frac{1}{2} \ln x + \ln 5$$

(b) 
$$\log_2 x + 4\log_2(x+1) - \frac{1}{3}\log_2(x-1)$$

(c) 
$$5\ln x + 2\ln 3 - 3\ln\left(\frac{1}{y}\right)$$

(2) Use the rules of logarithms to expand the following expressions so that there are no logarithms of products, quotients, or powers.

(a) 
$$\ln \sqrt[3]{x^3y}$$

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(b) 
$$\log_{10} \frac{10}{4x^2}$$

(c) 
$$\ln\left(\frac{x\sqrt{y}}{(1+x)^3}\right)$$

- (3) Suppose  $\ln x = 2$ ,  $\ln y = 3$  and  $\ln z = 6$ . Evaluate the following.
  - (a)  $\ln(xyz)$

(b) 
$$\ln(x^2 y)$$

(c) 
$$\ln\left(\frac{x^3}{\sqrt{z}}\right)$$